

MATHEMATICAL TABLES

Integrals Containing Logarithmic Functions

$\int \ln x \, dx = x \ln x - x + c$
$\int (\ln x)^2 \, dx = x (\ln x)^2 - 2x \ln x + 2x + c$
$\int (\ln x)^3 \, dx = x (\ln x)^3 - 3x (\ln x)^2 + 6x \ln x - 6x + c$
$\int (\ln x)^n \, dx = x (\ln x)^n - n \int (\ln x)^{(n-1)} \, dx, \text{ for } n \neq -1$
$\int \frac{dx}{\ln x} = \ln(\ln x) + \ln x + \frac{(\ln x)^2}{2.2!} + \frac{(\ln x)^3}{3.3!} + \dots + c$
$\int \frac{dx}{(\ln x)^n} = \frac{-x}{[(n-1)(\ln x)^{(n-1)}]} + \frac{1}{(n-1)} \int \frac{dx}{(\ln x)^{(n-1)}, \text{ for } n \neq 1$
$\int x^m \ln x \, dx = x^{(m+1)} \left[\frac{(\ln x)}{(m+1)} - \frac{1}{(m+1)^2} \right] + c, \text{ for } m \neq -1$
$\int x^m (\ln x)^n \, dx = \frac{[x^{(m+1)} (\ln x)^n]}{(m+1)} - \frac{n}{(m+1)} \int x^m (\ln x)^{(n-1)} \, dx \text{ for } m \neq -1, n \neq -1$
$\int \frac{(\ln x)^n}{x} \, dx = \frac{(\ln x)^{(n+1)}}{(n+1)} + c$

Integrals Containing Inverse Hyperbolic Functions

$\int \operatorname{sh}^{-1} \frac{x}{a} \, dx = x \operatorname{sh}^{-1} \frac{x}{a} - \sqrt{(x^2 + a^2)} + k$
$\int \operatorname{cosh}^{-1} \frac{x}{a} \, dx = x \operatorname{cosh}^{-1} \frac{x}{a} - \sqrt{(x^2 - a^2)} + k$
$\int \operatorname{tanh}^{-1} \frac{x}{a} \, dx = x \operatorname{tanh}^{-1} \frac{x}{a} + \frac{a}{2} (a^2 - x^2) + k$
$\int \operatorname{coth}^{-1} \frac{x}{a} \, dx = x \operatorname{coth}^{-1} \frac{x}{a} + \frac{a}{2} \ln(x^2 - a^2) + k$